

Manisa

Magnesia ad Sypilum

priene, Ephesus and Troalles (Pegon) trade route

"don't forget the way home"

Magnets have two poles,

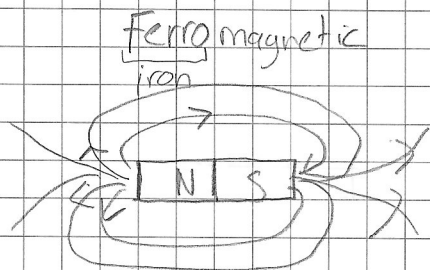
the one that points towards north \rightarrow north pole N

the one that points toward south \rightarrow south pole S

Similar poles repulse, opposite poles attract

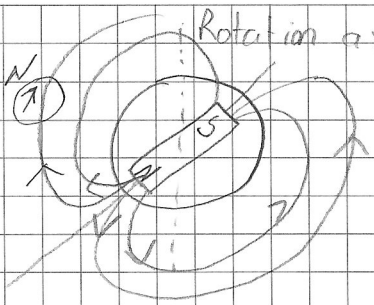
if you split a magnet in two, you still have N and S poles, No magnetic monopole has ever been observed.

Only iron, and a few other materials such as Cobalt, nickel, gadolinium, and some of their oxides show strong magnetic fields



- Magnetic field is tangent to the field line
- Intensity is proportional to the # field lines

Magnetic field always forms loops (no monopole)
direction: North pole side of the compass



earth magnetic field

north magnetic pole → south pole of earth's magnetic field

north magnetic pole ≠ geographic north pole

geomagnetic ↗

rotation axis ↓

Since the magnetic field lines are not parallel to the surface → "angle of dip" is the angle btw field line and horizontal

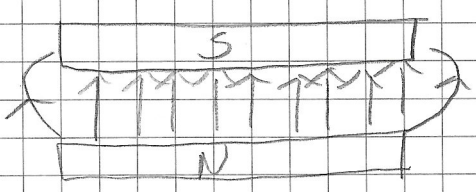
the difference btw geographical north and geomagnetic north has to be taken into account → magnetic declination (magnetic maps)

Uniform magnetic field

Simplest form of magnetic field

does not change from one point to another

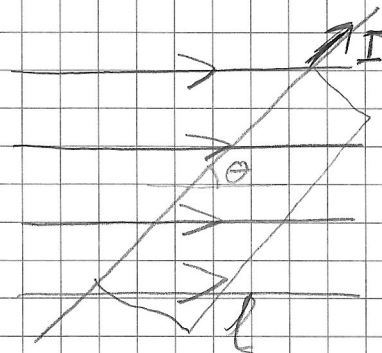
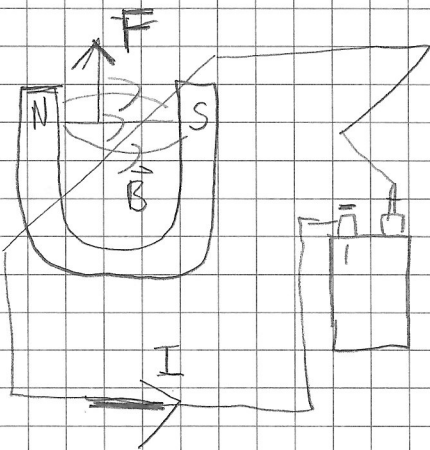
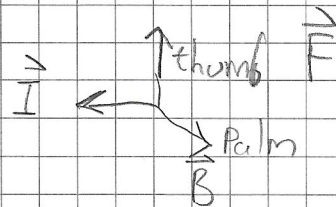
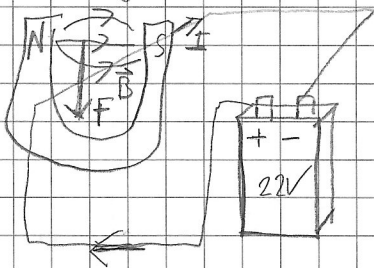
not easy to produce



Electric currents and magnetic fields

1820 Hans Christian Oersted
 an electric current produces
 a magnetic field

right-hand rule



$$F = I l B \sin \theta$$

$$\vec{F} = I \vec{l} \times \vec{B}$$

where \vec{l} is a vector along the current
 direction with magnitude equal to the length
 of wire exposed to the magnetic field

Generalisation

$$d\vec{F} = I d\vec{l} \times \vec{B}$$

(This can serve as a practical definition
 of \vec{B})

The SI unit for magnetic field B is Tesla

earth $\rightarrow 0.5 \times 10^{-4} T$

refrigerator $\rightarrow 0.01 T$

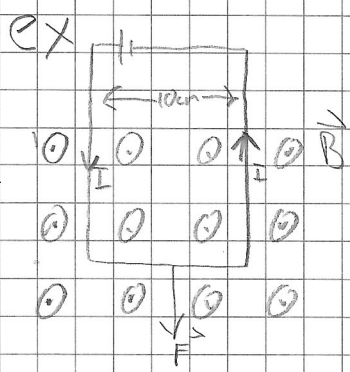
MR $\rightarrow 2T$ (can hold paper)

ex Magnetic force on a current-carrying wire
30A current $l = 12cm$ exposed to \vec{B} at $\theta = 60^\circ$
0.90T

$$F = I l B \sin \theta = (30A)(0.12m)(0.90T)(0.866) = 2.8N$$

Diagram note

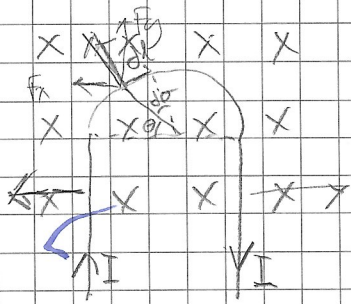
- ⊙ tip of an arrow towards you out from paper
- ⊗ back of an arrow moving away



$I = 0.245A$ $\vec{F} = 3.48 \times 10^{-2} N$
what is \vec{B}

force from left and right cancel out
only lower part contributes

$$B = \frac{F}{I l \sin 40} = \frac{3.48 \times 10^{-2} N}{(0.245 A)(0.1 m)} = 1.02 T$$



the left and right wires carry I & B_0 to opposite directions

length of infinitesimal wire of the curve

$$|d\vec{l}| = R d\phi$$

the angle of $d\vec{l}$ wire with $\vec{B} = 90^\circ$

$$d\vec{F} = I d\vec{l} \times \vec{B} \rightarrow dF = I R B d\phi$$

$$F_x = \int_0^\pi dF \cos\phi \rightarrow 0 \quad (\text{symmetric integral})$$

$$F_y = \int_0^\pi dF \sin\phi = I B_0 R \int_0^\pi \sin\phi = -I B_0 R \cos\phi \Big|_0^\pi = 2 I B_0 R$$

Up towards +y

Force on an electric charge moving in magnetic field

$$I = Nq/t$$

l : length q travels in \vec{B}

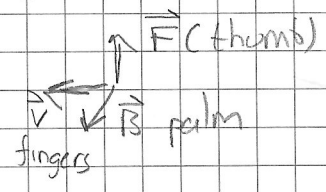
$$\vec{l} = \vec{v} t$$

$$\vec{F} = I \vec{l} \times \vec{B} = \frac{Nq}{t} (\vec{v} t) \times \vec{B} = Nq \vec{v} \times \vec{B}$$

$$\boxed{\vec{F} = q \vec{v} \times \vec{B}}$$

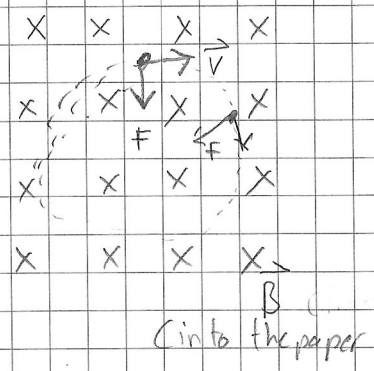
$$F = qvB \sin \theta \quad \theta = 90 \text{ max}$$

Right hand rule



question will ~~at~~ rest move near a magnet
No

Path of a charged particle in uniform \vec{B} field



force is always perpendicular to \vec{v} so $|\vec{v}|$ does not change
 since $|\vec{v}|$ is always the same but the charge is being deflected
 \rightarrow circular path, centripetal acceleration
 $a = \frac{v^2}{r}$

$$\sum F = ma$$

$$\uparrow \qquad \uparrow$$

$$qVB \qquad m \frac{v^2}{r}$$

$$r = \frac{mv}{qB}$$

the time it takes for the charge to turn:

$$T = \frac{2\pi r}{v} = \frac{2\pi m}{qB}$$

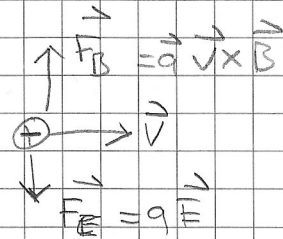
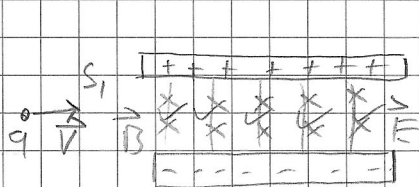
frequency $f = \frac{1}{T} = \frac{qB}{2\pi m} \rightarrow$ cyclotron frequency

The Lorentz equation

$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$

It is a basic equation in physics

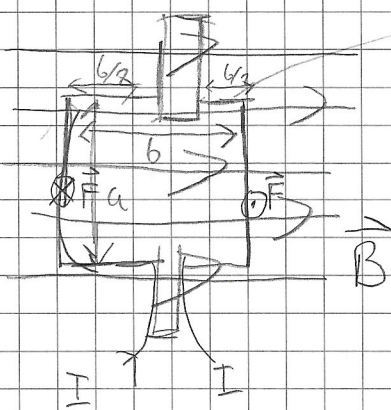
Velocity selector



if $\vec{F}_B = \vec{F}_E$ particle crosses the filter

$$qvB = qE \Rightarrow v = \frac{E}{B} \quad (\text{does not depend on } q)$$

Torque on a current loop



$\theta = 0 \rightarrow$ no force

$$\begin{aligned} |\vec{\tau}| &= I a B \frac{b}{2} + I a B \frac{b}{2} = I a B b \\ &= I A B \end{aligned}$$

↑
area

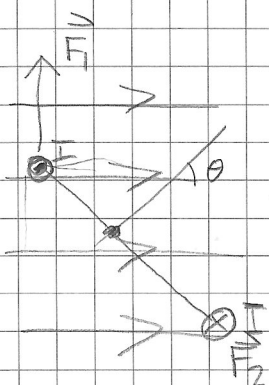
N loops \rightarrow

$$|\vec{\tau}| = N I A B$$

length of the lever arm

$$\text{is } \frac{b}{2} \sin \theta$$

$$\tau = N I A B \sin \theta$$



magnetic dipole moment is defined as

$$\vec{\mu} = N I \vec{A}$$

↓ unit norm of the plane

so, torque is

$$\vec{\tau} = N I \vec{A} \times \vec{B}$$
$$\boxed{\vec{\tau} = \vec{\mu} \times \vec{B}}$$

$$U = \int \tau d\theta = \int N I A B \sin\theta d\theta = -\mu B \cos\theta + C$$

$$U=0 \text{ at } \theta = \pi/2 \rightarrow C = 0 \text{ at } \theta = \pi/2$$

$$U = -\mu B \cos\theta = -\vec{\mu} \cdot \vec{B}$$

Torque on a circular coil

diameter 20.0 cm 10 loops 3.0 A

2.00 T magnetic field

max and min torque?

$$A = \pi r^2 = \pi (0.1)^2 \text{ m}^2 = 3.14 \times 10^{-2} \text{ m}^2$$

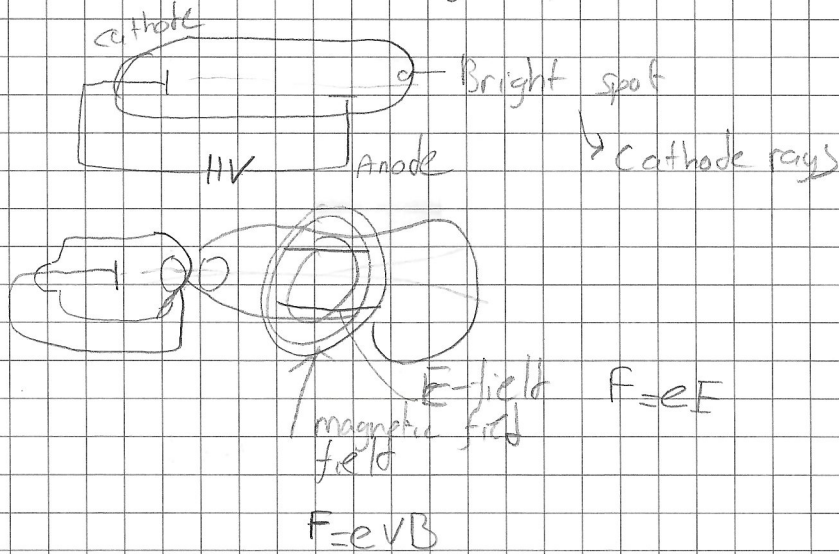
max torque $\theta = 90$ (face parallel to the \vec{B})

$$\tau = N I A B \sin\theta = (10) (3.00 \text{ A}) (3.14 \times 10^{-2} \text{ m}^2) (2.00 \text{ T})$$
$$= 1.188 \text{ N}\cdot\text{m}$$

min torque $\theta = 0$ $\tau = 0$

Discovery of the electron

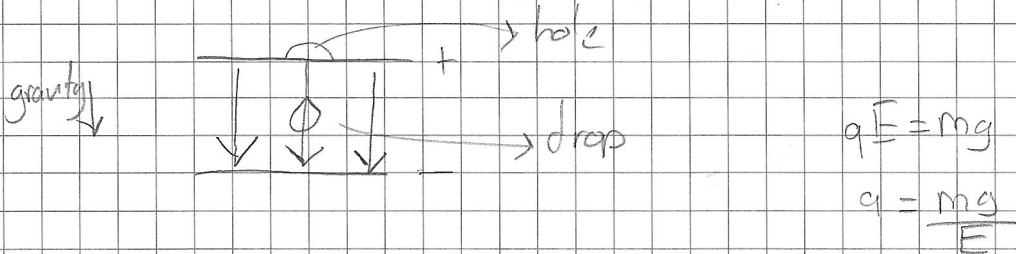
1890s (e^- age?)



$$e v B = \frac{m v^2}{r} \rightarrow \frac{e}{m} = \frac{v}{B r}$$

$$F = eE = e v B \quad v = \frac{E}{B} \quad \frac{e}{m} = \frac{E}{B^2 r}$$

Milikan oil-drop experiment



terminal velocity \rightarrow mass of the droplet

long experiments \rightarrow unit of charge $1.6 \times 10^{-19} \text{ C}$

$$\frac{e}{m} = \frac{1.6 \times 10^{-19} \text{ C}}{m} = 1.76 \times 10^{11} \text{ C/kg}$$

$$m_e = 9.11 \times 10^{-31} \text{ kg} \quad (\text{thus } e \text{ is a part of } e^-)$$

1/1000th of H mass

The Hall effect

Nobels

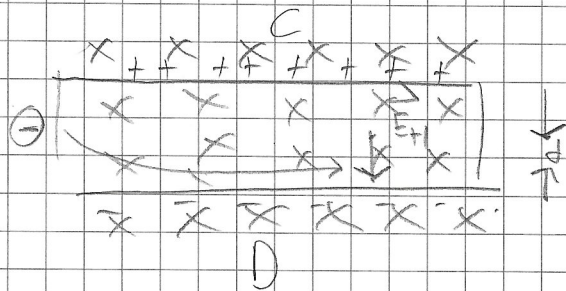
1985 → quantized hall effect

1998 → fractional charged excitations

2016 → topological phases

2010 → graphene

Edwin H Hall observed an unexpected electrical phenomenon in 1879



when a current carrying conductor is in a magnetic field the electrons move towards one of the faces

$$\vec{F}_B = e \vec{v}_d \times \vec{B}$$

This creates an electric potential difference btw two sides until

$$eE_H = e v_d B$$

Hall emf is

$$E_H = E_H d = v_d B d \quad \text{where } d = \text{width}$$

Hall probe → measures strength of magnetic fields